**Trying Triangulars**

The triangular numbers are 1, 3, 6, 10, ...

17 can be expressed as the sum of distinct triangular numbers:   
17 = 1 + 6 + 10.

5 cannot be expressed as the sum of distinct triangular numbers.

What is the largest positive integer that cannot be expressed as the sum of distinct triangular numbers?